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Theoretical results for top-quark cross sections and distributions

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I present new results and updates for total cross sections and differential distributions in topantitop pair and single-top production. Soft-gluon corrections are added to exact fixed-order results to provide the best predictions at approximate N^3LO for $t\bar{t}$ production and approximate NNLO for single-top production. Total cross sections and top-quark transverse-momentum and rapidity distributions are presented and compared with data at LHC and Tevatron energies. The cusp anomalous dimension at three and higher loops is also discussed.

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1. Top-pair cross sections and differential distributions

QCD corrections to $t\bar{t}$ production are quite substantial. Soft-gluon corrections are a very important subset of the corrections and they approximate exact results very well. In fact, the higher-order results through NNLO have been very well predicted in the past by the evaluation of the soft-gluon contributions [1]. These soft corrections were calculated from resummation at NNLL accuracy for the double-differential cross section. Approximate N³LO (aN³LO) predictions for cross sections were later derived [2] by adding the third-order soft-gluon corrections.

The aN³LO $t\bar{t}$ cross sections and top-quark differential distributions in p_T and rapidity were calculated in [2], and numerical results were presented using MSTW2008 NNLO pdf [3]. The cross sections increase somewhat if one uses the more recent MMHT2014 pdf [4]. For a top quark mass $m_t = 173.3$ GeV the aN³LO total cross section using MMHT2014 NNLO pdf is 826^{+24+14}_{-16-18} pb at 13 TeV LHC energy and 975^{+28+16}_{-19-20} pb at 14 TeV LHC energy, where the indicated uncertainties are from scale variation by a factor of two around $\mu = m_t$, and from the pdf at 68% C.L.

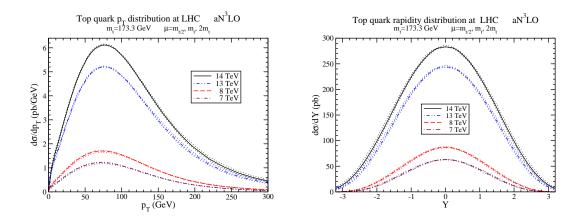


Figure 1: Top-quark aN 3 LO p_T (left) and rapidity (right) distributions at LHC energies.

In Fig. 1 we plot theoretical results, including scale variation, for the aN³LO differential distributions in transverse momentum and rapidity of the top quark at 7, 8, 13, and 14 TeV LHC energies.

In Fig. 2 we plot theoretical results for the aN³LO differential distributions in transverse momentum of the top quark at 8 and 13 TeV energies and compare with CMS data [5], finding excellent agreement between theoretical predictions and data in both cases.

In Fig. 3 we plot theoretical results for the aN³LO normalized differential distributions in rapidity of the top quark and compare with CMS data at 8 and 13 TeV energies [6], again finding excellent agreement between theory and data.

Higher-order corrections are very sizable for the $t\bar{t}$ total cross sections and also for the differential distributions. Given the large contributions from higher orders and the relatively slow convergence of the perturbative series, it is clear that NNLO calculations are not enough; the inclusion of aN³LO contributions is needed for truly precision top-quark physics.

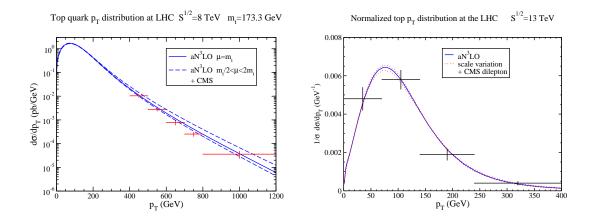


Figure 2: Top-quark aN 3 LO p_T distributions at 8 TeV (left) and 13 TeV (right) LHC energies compared with CMS data [5].

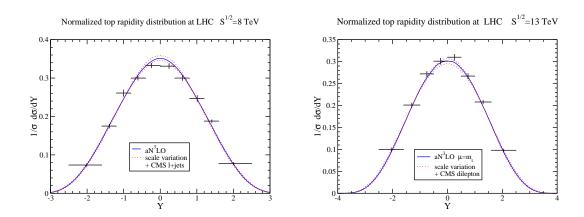


Figure 3: Top-quark aN³LO rapidity distributions at 8 TeV (left) and 13 TeV (right) LHC energies compared with CMS data [6].

2. Single-top cross sections and differential distributions

Single-top production processes include the *t*-channel via $qb \to q't$ and $\bar{q}b \to \bar{q}'t$; the *s*-channel via $q\bar{q}' \to \bar{b}t$; and associated tW production via $bg \to tW^-$.

The aNNLO cross sections for all three processes were calculated in Ref. [7], and results are plotted in Fig. 4 with MSTW2008 pdf. We observe excellent agreement of theory with Tevatron and LHC data for the *t*-channel [8, 9], the *s*-channel [10], and the *tW* channel [11].

The numbers increase a bit when MMHT2014 pdf are used. For the *t*-channel at the 13 TeV LHC using MMHT2014 NNLO pdf [4] and $m_t = 173.3$ GeV, we find cross sections of $138^{+3}_{-1} \pm 2$ pb for the top and $83^{+2}_{-1} \pm 1$ pb for the antitop, giving $221^{+5}_{-2} \pm 3$ pb for the sum. At 14 TeV we find $157^{+4}_{-1} \pm 2$ pb for the top, $95^{+2}_{-1} \pm 1$ pb for the antitop, and $252^{+6}_{-2} \pm 3$ pb for the sum.

For the s-channel at 13 TeV LHC energy with MMHT2014 pdf we find cross sections of

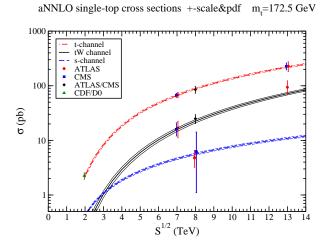


Figure 4: aNNLO single-top cross sections in t-channel, s-channel, and tW processes compared with Tevatron [8] and LHC [9, 10, 11] data at various energies.

 $7.15\pm0.13^{+0.15}_{-0.17}$ pb for the top and $4.14\pm0.05\pm0.10$ pb for the antitop, giving $11.29\pm0.18\pm0.26$ pb for the sum. At 14 TeV we find $7.83\pm0.14\pm0.18$ pb for the top, $4.60\pm0.05\pm0.11$ pb for the antitop, and $12.43\pm0.19\pm0.29$ pb for the sum.

For tW^- production we find a cross section at 13 TeV of $36.3 \pm 0.9 \pm 0.9$ pb and at 14 TeV of $42.8 \pm 1.0 \pm 1.1$ pb with MMHT2014 pdf. The numbers are the same for $\bar{t}W^+$ production.

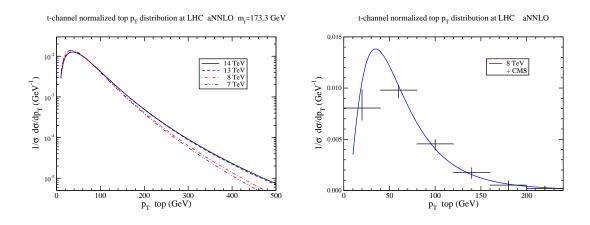


Figure 5: aNNLO top-quark normalized p_T distributions in t-channel production at LHC energies (left) and comparison to CMS data [12] at 8 TeV energy (right).

In Fig. 5 we plot the aNNLO top-quark normalized p_T distributions in t-channel production at LHC energies (left plot) and compare with CMS data [12] at 8 TeV (right plot).

3. Cusp anomalous dimension

The cusp anomalous dimension is an essential ingredient in higher-order calculations and resummations of soft-gluon contributions in perturbative cross sections. In particular, it is the simplest soft anomalous dimension, and a component of soft anomalous dimensions for more complicated color processes, such as $t\bar{t}$ production. Its perturbative expansion can be written as $\Gamma_{\text{cusp}} = \sum_{n=1}^{\infty} (\alpha_s/\pi)^n \Gamma^{(n)}$ [13, 14, 15, 16]. Some diagrams are shown in Fig. 6.

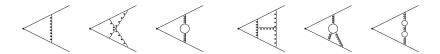


Figure 6: Some of the one-loop, two-loop, and three-loop diagrams for the cusp anomalous dimension.

The cusp angle is $\theta = \cosh^{-1}(v_i \cdot v_j / \sqrt{v_i^2 v_j^2})$ where v_i and v_j are heavy-quark velocity vectors. We have $\Gamma^{(1)} = C_F(\theta \coth \theta - 1)$ and [14]

$$\Gamma^{(2)} = \frac{K}{2} \Gamma^{(1)} + \frac{1}{2} C_F C_A \left\{ 1 + \zeta_2 + \theta^2 - \coth \theta \left[\zeta_2 \theta + \theta^2 + \frac{\theta^3}{3} + \operatorname{Li}_2 \left(1 - e^{-2\theta} \right) \right] + \coth^2 \theta \left[-\zeta_3 + \zeta_2 \theta + \frac{\theta^3}{3} + \theta \operatorname{Li}_2 \left(e^{-2\theta} \right) + \operatorname{Li}_3 \left(e^{-2\theta} \right) \right] \right\}.$$

The three-loop result was first derived in [15]. In Ref. [16] it was expressed in the form

$$\Gamma^{(3)} = C^{(3)} + K^{'(3)}\Gamma^{(1)} + K \left[\Gamma^{(2)} - \frac{K}{2}\Gamma^{(1)} \right]$$

where $C^{(3)}$ was given in terms of ordinary polylogarithms.

From the structure of Γ_{cusp} through three loops, an *n*-loop conjecture was put forth in [16]:

$$\Gamma^{(n)} = \sum_{k=1}^{n} \frac{(n-1)!}{(k-1)! (n-k)!} K^{'(k)} C^{(n-k+1)}.$$

Simple yet excellent numerical approximations to the exact results can be derived. We find, for $n_f = 5$ and with $\beta = \tanh(\theta/2)$, the simple formulas [16]

$$\Gamma^{(2)}_{\rm approx}(\beta) = -0.38649\,\beta^2 + 1.72704\,\Gamma^{(1)}(\beta)\,; \quad \Gamma^{(3)}_{\rm approx}(\beta) = 0.09221\,\beta^2 + 2.80322\,\Gamma^{(1)}(\beta)\,.$$

In Fig. 7 we plot the cusp anomalous dimension and its approximations through third order.

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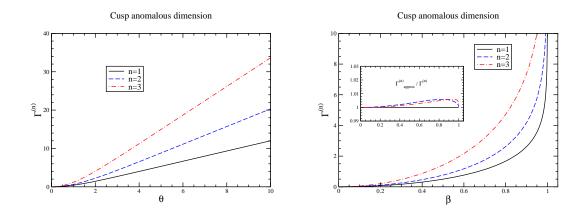


Figure 7: The cusp anomalous dimension at one, two, and three loops.

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